

Solve the following equations over the interval $[0, 2\pi)$.

1. $2\cos x + \sqrt{3} = 0$

$$\cos x = -\frac{\sqrt{3}}{2}$$

$$x = \frac{5\pi}{6}, \frac{7\pi}{6}$$

2. $4\sin\theta - 1 = 2\sin\theta$

$$2\sin\theta - 1 = 0$$

$$\sin\theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{6}, \frac{5\pi}{6}$$

3. $3\sin\theta + 5 = -2\sin\theta$

$$5\sin\theta + 5 = 0$$

$$\sin\theta = -1$$

$$\theta = \frac{3\pi}{2}$$

4. $\sin^2\theta - 1 = 0$

$$\sin^2\theta = 1$$

$$\sin\theta = \pm 1$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

5. $9\tan^2 x - 3 = 0$

$$\tan^2 x = \frac{1}{3}$$

$$\tan x = \pm\sqrt{\frac{1}{3}} = \pm\frac{\sqrt{3}}{3}$$

$$x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$$

6. $4\sec^2 x - 2 = 0$

$$\sec^2 x = \frac{1}{2}$$

$$\cos^2 x = 2$$

$$\cos x = \pm\sqrt{2} \approx \pm 1.4 \rightarrow \text{undefined for cos}$$

$$\text{No solution}$$

For the following, round your answers to 4 decimals.

7. $\sin x = .8246$

$$x = \sin^{-1}(.8246)$$

$$x = .9695$$

 ≈ 0

$$x = \pi - .9695$$

$$x = .9695, 2.1712$$



8. $\cos x = -\frac{2}{5}$

$$x = \cos^{-1}(\frac{2}{5})$$

$$= 1.9823$$

 ≈ 0

$$x = 2\pi - 1.9823$$

$$x = 1.9823, 4.3009$$



$$x = 2\pi - 1.9823$$

9. $\tan x = -3$

$$x = \tan^{-1}(-3)$$

$$= -1.1071$$

 ≈ 0

$$x = \pi + 1.8925$$

$$x = 1.8925, 5.0341$$

