

$$E = hf \quad h = 6.63 \times 10^{-34} \text{ J}\cdot\text{s}$$

$$c = f\lambda \quad c = 3.00 \times 10^8 \text{ m/s}$$

Name STURMAN KEY
 Period _____ Date _____

Sample Light Energy Problems

1. Find the smallest increment of energy that a water molecule can absorb from a single microwave photon, wavelength $4.00 \times 10^6 \text{ nm}$.

$$\begin{aligned} \lambda &= 4.00 \times 10^6 \text{ nm} \\ &= 4.00 \times 10^6 \times 10^{-9} \text{ m} \\ &= 4.00 \times 10^{-3} \text{ m} \end{aligned}$$

$$\begin{aligned} c &= f\lambda \\ 3.00 &= f(4.00 \times 10^{-3}) \\ f &= \underline{7.50 \times 10^{10} \text{ s}^{-1}} \end{aligned}$$

$$\begin{aligned} E &= 6.63 \times 10^{-34} (7.50 \times 10^{10}) \\ &= \underline{4.97 \times 10^{-23} \text{ J}} \end{aligned}$$

2. Find the wavelength, in nm, of a photon that gives off $7.53 \times 10^{-20} \text{ J}$ of energy.

$$\begin{aligned} E &= 7.53 \times 10^{-20} \text{ J} \\ \lambda &= ? \text{ nm} \end{aligned}$$

$$\begin{aligned} E &= hf \\ 7.53 \times 10^{-20} &= 6.63 \times 10^{-34} f \\ f &= \underline{1.14 \times 10^{14} \text{ s}^{-1}} \end{aligned}$$

$$\begin{aligned} c &= f\lambda \\ 3.00 \times 10^8 &= 1.14 \times 10^{14} \lambda \\ \lambda &= 2.63 \times 10^{-6} \text{ m} \\ &= 2.63 \times 10^{-6} \times 10^9 \text{ nm} \\ &= \underline{2.63 \times 10^3 \text{ nm or } 2630 \text{ nm}} \end{aligned}$$

3. Compare the energy entering your eyes, per photon, for blue sunglasses and red sunglasses.

Blue
 $\lambda = 450 \text{ nm}$
 $= 450 \times 10^{-9} \text{ m}$

Red
 $\lambda = 750 \text{ nm}$
 $= 750 \times 10^{-9} \text{ m}$

Blue
 $c = f\lambda$
 $3.00 \times 10^8 = f(450 \times 10^{-9})$
 $f = 6.67 \times 10^{14} \text{ s}^{-1}$
 $E = 6.63 \times 10^{-34} (6.67 \times 10^{14})$
 $= \underline{4.42 \times 10^{-19} \text{ J}}$

Red
 $c = f\lambda$
 $3.00 \times 10^8 = f(750 \times 10^{-9})$
 $f = 4.00 \times 10^{14} \text{ s}^{-1}$
 $E = 6.63 \times 10^{-34} (4 \times 10^{14})$
 $= \underline{2.65 \times 10^{-19} \text{ J}}$

Blue $\frac{4.42 \times 10^{-19}}{2.65 \times 10^{-19}}$
Red $\frac{2.65 \times 10^{-19}}{2.65 \times 10^{-19}} = 1.67$
 Blue emits 1.67x more energy into your eye!

4. A carbon dioxide laser used in surgery has a frequency of 30 GHz. What is the energy of a single photon emitted from this laser?

$$\begin{aligned} f &= 30 \text{ GHz} \\ &= 30 \times 10^9 \text{ Hz} \end{aligned}$$

$$\begin{aligned} E &= hf = \\ &= 6.63 \times 10^{-34} (30 \times 10^9) = 1.989 \times 10^{-23} \Rightarrow \underline{2.0 \times 10^{-23} \text{ J}} \end{aligned}$$

5. If this laser emits $1.0 \times 10^4 \text{ J}$ of energy every second, then how many photons are emitted each second?

$$\frac{1.0 \times 10^4 \text{ J}}{1 \text{ s}} \cdot \frac{1 \text{ photon}}{2.0 \times 10^{-23} \text{ J}} = \underline{5.0 \times 10^{26} \text{ photons/sec}}$$

6. Satellite dishes are designed to receive waves of 3.90 m. What is the frequency of these waves in MHz?

$$\begin{aligned} \lambda &= 3.90 \text{ m} \\ c &= 3.00 \times 10^8 \text{ m/s} \\ f &= ? \text{ MHz} \end{aligned}$$

$$\begin{aligned} c &= f\lambda \\ 3.00 \times 10^8 &= f(3.90) \\ f &= \underline{7.69 \times 10^7 \text{ Hz}} \end{aligned}$$

$$\begin{aligned} \frac{7.69 \times 10^7 \text{ Hz}}{1} \cdot \frac{1 \text{ MHz}}{10^6 \text{ Hz}} \\ &= \underline{7.69 \times 10^1 \text{ MHz}} \\ &\text{or } \underline{76.9 \text{ MHz}} \end{aligned}$$

(5)